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The Use of Rasch Modeling To Improve Standard Setting

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> This paper examines four ways in which Rasch modeling may be used to improve standard setting. The first three methods are applied to the Angoff procedure and the fourth is an example of bookmarking. Using an actual data set taken from the New South Wales School Certificate test in Mathematics, worked examples are provided that show how informative data may be provided to the judges, both before and after they Angoffrate the test items. In addition, an example of bookmarking is given, along with a variant of the latter known as item mapping. The application of non Rasch IRT procedures to standard setting is also discussed.

Standard setting is now a fundamental goal for reporting educational outcomes in many education systems around the world. It is in widespread use across the US in state testing systems and is used in the UK. In Australia, it is used in all the Year 10 and Year 12 examinations in the New South Wales (NSW) education system (Board of Studies NSW, 2003). The two most popular procedures for standard setting are the Angoff method (Angoff, 1971) and a newer procedure, the Bookmark method (Mitzel, Lewis, Patz and Green, 2001).

Standard setting involves a systematic set of procedures that identifies a common judgement as to the cut score required for a given level of proficiency. It would be naïve to think that such procedures identify a "true" standard which proficiency non-proficiency. separates from Standards are in an obvious sense arbitrary, being influenced by the perceived characteristics of the examinees, the educational experiences and values of the particular judges and the expectations of the society from which the judges are drawn. The arbitrary nature of standards, however, does not

mean they are capricious, and does not negate the educational benefits that may flow from their establishment. The most important requirement of such standard-setting procedures is that of consistency—once consensus among the judges is reached, the procedures should classify the same type of students as being proficient across different occasions, test instruments, judging panels and so on.

While the Angoff method was originally conceived as a one-stage test-centered process, it has now typically developed into a multi-stage procedure in which the judges make independent judgements and then discuss their initial decisions. This group discussion process has been advocated by several researchers (for example, Jaeger, 1982; Norcini, Lipner, Langdon and Strecker, 1987; Morrison, Busch and D'Arcy, 1994; Berk, 1996). In the discussion phase it is customary to provide the judges with data on the accuracy of their initial decisions. Providing the judges with such data has been suggested by Popham (1978), Linn (1978), Cross, Impara, Frary and Jaeger (1984), and

Norcini, Shea and Kanya (1988). There is a natural affinity between IRT models and many standardsetting procedures, with a shared view of a continuum of achievement and a probabilistic definition of mastery on an item. Both van der Linden (1982) and Kane (1987) have discussed the similarities between IRT models and Angoff standard-setting procedures.

Given that standard setting in certification has high stakes for individuals, there is considerable interest in understanding the process and in finding ways to reduce variability in standard setting from occasion to occasion (MacCann and Stanley, 2004). Using a data set taken from a state-wide standardsetting operation, this paper will illustrate some ways in which Item Response Theory (IRT) can be used to provide feedback to help judges in both the Angoff and Bookmarking procedures.

THE SCHOOL CERTIFICATE MATHEMATICS PROGRAM

To show the ways in which Rasch modeling can be used to improve standard setting, data based on a multi-stage Angoff procedure will be analysed. The test comprised 50 short items, which were dichotomously scored—0 for a wrong answer, 1 for the correct answer. The test items came from the School Certificate Mathematics external test program, which tests the fundamental knowledge and skills of students in Year 10 in New South Wales (generally of age 15-16 years). Approximately 78,000 students attempt this compulsory test, but the analyses below were based on a simple random sample of 10,000 students. This program uses a three-stage Angoff procedure with six experienced teacher-judges to allocate each student to one of six performance bands. The highest band, Band 6, which generally corresponds to the top 3-10% of students, will be used for the purposes of illustration in this paper.

ITEM RESPONSE THEORY

IRT developed from the initial work of Lord (1952, 1953) on latent trait models and the independent development by Rasch of the one-

parameter model (Rasch, 1960, 1966). In contrast to Classical Test Theory (CTT), IRT uses relatively strong assumptions but produces a measurement scale that has a number of advantages over CTT and now holds a central place in educational measurement theory. For expositions of IRT and the various models that have been developed see Lord (1980), Hambleton, Swaminathan and Rogers (1991), van der Linden and Hambleton (1997), Embretson and Reise (2000).

In the NSW education system, the oneparameter Rasch model is widely used to analyse tests. The Rasch model software package employed in this paper is RUMM—Rasch Unidimensional Measurement Models (Andrich, Sheridan, Lyne and Luo, 2000). The Rasch model is the simplest of the IRT models, having only one parameter to describe an item—its difficulty. In addition, each person has one parameter to describe their performance—their ability.

The RUMM software accepts the usual type of data file where the student records are in rows and the test items are in columns. Applying the appropriate mathematical modeling to this data matrix, the software produces a person ability estimate for each student, and an item difficulty estimate for a test item. These estimates are on the *logit* scale (log odds units), a scale arbitrarily centred on zero for the difficulty of the test items, and theoretically ranging from minus infinity to plus infinity. (In practice most estimates fall in the –4 to +4 range.)

The relationship between total score and ability in logits

For the case of all items being compulsory (as they are in School Certificate Mathematics), and for the one parameter logistic model, the total score is a sufficient statistic for estimating a student's ability level (Andersen, 1973). This implies that every examinee on the same total score will receive the same ability estimate. The relationship between the total score and the ability estimate is shown below in Figure 1.



Figure 1: Conversion from total score to ability in logits

A conversion table like this should be obtainable from all reputable Rasch software packages. Note that the conversion is relatively linear for a large part of the mark range, but increases sharply in the upper mark range. A few marks total score difference in the upper mark range results in a larger ability difference than would occur for the same total score difference near the middle of the distribution. Similarly, the conversion decreases sharply at the bottom of the mark range. For students scoring full marks (50), or zero marks, ability estimates are hard to justify, although some software packages give such estimates.

This conversion between total score and ability (and vice versa) is frequently used in the procedures to follow.

ANGOFF PROCEDURES

In the Angoff method, a panel of judges is assembled which is representative of the community that works with and interprets the standards. In the NSW system, this comprises six experienced teachers. For the traditional Angoff method, each judge works through the test items *independently*, estimating the probability of success on each item for the candidates under consideration. In practice, rather than express the task in terms of probabilities, the judges are usually asked to envisage a group of such candidates and to estimate the proportion of the group who would succeed on the item. This results in a series of Angoff-ratings for each judge. When these ratings are regarded as final, they are *summed* over all the items in the test to produce a *total cut score* for the judge. A final total cut score is obtained by averaging across the judges' total cut scores. This is the Angoff method in its basic state.

This basic procedure has typically evolved into a multi-staged process in most systems. Whereas the judges work independently in the first stage described above, in the later stages the judges usually collaborate and receive some form of feedback on the accuracy of their judgements. Thus, the judges usually get to modify their judgements before they become final and are summed over items and averaged across judges. In addition, material is often provided to help the judges formulate an image of the desired candidates who are proficient at the given level. For example, if the system has been in operation for some years, "Standards Packages" on CD-Rom may be made available for the judges to study. These typically contain test items from previous years showing the success rates obtained by candidates near the total cut score.

In the sections below, it will be shown how Rasch modeling can assist the judges in forming and modifying their Angoff-ratings.

Data which assists the judges to make item probability estimates

This section deals with the Angoff procedures and illustrates the type of information that could be given to the judges before they give Angoff probability ratings to each item. Firstly, the test is analysed via IRT to produce item difficulty estimates and person ability estimates. The relationship between a total score on the 50 items and person ability is given in Figure 1. From this figure, given a total score, an ability can be determined. Then given the person ability and the difficulty of the item, the probability of success on item *j* by person *i* is given by

$$P_{ij} = \frac{1}{1 + e^{-(\theta_i - \beta_j)}} \ . \tag{1}$$

where θ_i is the ability of person *i*, and β_j is the difficulty of item *j*.

(Note that there are other forms of this equation. For example, it is sometimes written

$$P_{ij} = \frac{1}{1 + e^{-D\overline{a}(\theta'_i - \beta'_j)}},$$

where *D* is a scaling constant, \overline{a} is a common level of discrimination for all items and their product may be termed the *scaling factor*. By letting $\theta_i = D\overline{a}\theta'_i$ and $\beta_j = D\overline{a}\beta'_j$, the scaling factor is absorbed into the ability and difficulty scale to create the simpler form of Equation 1.)

From Equation 1 a table can be generated which shows how students on a particular total score would be expected to perform on each item, as in Table 1 below. This table could be provided to the judges before they attempt their Angoff ratings. To save space, it is shown here for a range of total scores surrounding the expected cut score and only for the first four items in the test. It gives the probability that students at a given score level would correctly answer the item. No probability estimates are given for a perfect score of 50 as this represents a ceiling that may distort the value of any attempted estimate.

For example, according to the IRT model, of the students scoring 45 (/50) on the total test, about 95% would be expected to be correct on Item 1, but only 72% would be expected to be correct on Item 2. In addition to providing information of students' expected performance on an item, this also provides a means of comparing the difficulty of the items at different ability levels. Clearly Item 2 is generally a much more difficult item than Item 1.

Comparing Item 1 with Item 3 gives little difference in the probability levels for students on a score of 47 (97% versus 94%), but this difference increases at lower ability levels. For example, for students on a score of 42, 92% are predicted to be correct on Item 1 but only 82% on Item 3.

In the approach considered here, Table 1 would be presented "upfront" to the judges. They would scan the Item 1 probability column and encircle the probability that best matched their Angoff-rating for Item 1. They would repeat this process for several items. If the encircled probabilities tended to fall on the same row, then they could stop when they were satisfied that the row reflected the standard of which they are thinking. Some judges may need only a small number of comparisons before settling on a row, while others may need to cover most of the items before then choosing the row that best fits the pattern of encircled probabilities. Once a row is tentatively chosen, the remaining items can be dealt with more quickly, as a confirmatory check, rather than performing Angoff ratings in isolation.

		IRT probability estimates			
Mark (/50)	Percentile	I1	I2	I3	I4
50	100.0	•			•
49	99.8	0.99	0.94	0.98	0.99
48	99.5	0.98	0.88	0.96	0.98
47	99.1	0.97	0.83	0.94	0.97
46	98.3	0.97	0.77	0.92	0.96
45	97.1	0.95	0.72	0.90	0.95
44	95.7	0.94	0.67	0.87	0.93
43	94.1	0.93	0.62	0.85	0.92
42	92.3	0.92	0.57	0.82	0.90
41	90.2	0.90	0.53	0.79	0.89
40	88.1	0.89	0.49	0.77	0.87
39	85.9	0.87	0.45	0.74	0.85
38	83.5	0.85	0.41	0.71	0.83
37	81.0	0.83	0.38	0.68	0.81
36	78.2	0.82	0.35	0.65	0.79
35	75.3	0.80	0.32	0.62	0.77
34	72.8	0.78	0.30	0.59	0.75
33	70.0	0.75	0.27	0.56	0.72
32	67.4	0.73	0.25	0.53	0.70
31	64.0	0.71	0.23	0.50	0.68
30	61.2	0.69	0.21	0.48	0.65

Table 1: IRT probability estimates for students at a given mark (ability) level for the first four items

For example, the actual (average) judges' ratings for the first four items are shaded in Table 1. It appears that even from this small amount of data, the standard desired is around a score of 42-43. Moreover, it is obvious which Angoff-ratings are aberrant, as in Item 2. This is a relatively difficult item, for which the judges have under-estimated the difficulty experienced by the Band 6 students. It is easy for the judges to see these discrepancies and to amend them. In this procedure, important data is presented "upfront" to the judges who can scan across a range of items to see the probabilities IRT has assigned and compare these probabilities with the estimates that they would have awarded. The item data is considered simultaneously and the judges can "home-in" on a row of the table, rather than the usual process of sequential item judgements, which can take much longer. The advantages of this process are a saving in time spent by the judges, the ease with which aberrant judgements may be spotted, and the fact that a

clearly stated model underlies the probability estimates in each row.

The item judgements can be selected in two ways. One would be for the judges to simply select the appropriate row of the table and to use the exact probabilities assigned by IRT. The second would be for the judges to select the appropriate row and to use the row to inform their probability estimates, but to enter their own probabilities that could differ from the IRT ones. The rationale for this would be that the IRT analysis is based on a model that is an approximation to reality and that the judges may prefer to rely on their experience of the past performance of similar students.

In addition to the IRT probabilities, normative data could be given—the percentile rank corresponding to each score level. For example students scoring 45 are at percentile 97.1 in the student population and about 95% of them would be expected to be correct on Q1 but only 72% on Q2, according to the IRT model. Such a table could be presented without the column giving the percentile rank. Reid (1991) has argued that the use of normative data in standards-setting needs to be carefully handled. Once the judges see the normative data, it may prove to be a dominant factor that biases the item judgements. On the other hand, Wiliam (1996) points out the danger that test-centered standards-setting procedures may lose touch with what students can actually do, resulting in set standards that are quite difficult to achieve.

The total cut score equivalents of each item judgement

In this section, the judges have Angoff-rated each item but have not yet summed the items to get a total cut score. Here feedback is given on the equivalent total cut score for each item. When the judges estimate a probability of success for an item, they are, in effect, setting an ability level. The item has a known *difficulty* level obtained from the IRT analysis and the judges are estimating a probability of success for cut score level type students. The estimated ability of the students at this cut score level is obtained by rearranging Equation 1 so that the person ability is a function of the probability of success on the item, giving:

$$\theta_i = \beta_j - \ln\left(\frac{1 - P_{ij}}{P_{ij}}\right). \tag{2}$$

where ln is the natural logarithm (logarithm to the base *e*).

The person ability is then converted to an equivalent total score on the test by using a conversion table similar to that graphed in Figure 1. For example, an ability of 2 logits translates to an expected total score of 41.4. This allows the generation of Table 2 below, which shows the expected total cut scores for the first 25 items.

Table 2 gives an item-by-item estimate of the total cut score. Instead of a single total cut score estimate based on an Angoff summing of item cut scores, there is a total cut score based on every item rating. Figure 2 below gives a boxplot of the estimated total cut scores from all 50 items. It shows that there is a wide range of estimates from 49 to 37 (/50), but the middle 50% of estimates lie between 45.5 and 40.5 approximately.

The data in Figure 2 may be instructive to the judges in several ways. Firstly, it indicates that an Angoff rating on a single item may give a wildly inappropriate result. Secondly, it gives a vivid way of indicating item estimates that seem to be anomalous. Thirdly, it indicates that there is a distribution of total cut score estimates and this suggests that there may be alternative methods of obtaining a final total cut score other than using the standard Angoff procedure of summing the item cut scores. The judges may reflect on this distribution of estimated total cut scores and choose an appropriate statistic. For example, in principle they could select the median of this set of scores, or some other measure, such as the 25th percentile, as reflecting the desired standard.

Item	Judges' Angoff	IRT ability	Corresponding
	rating	matching	total cut score
	C	Angoff rating	
1	0.91	2.005	41.4
2	0.82	3.315	46.8
3	0.83	2.133	42.1
4	0.92	2.329	43.1
5	0.98	2.731	44.9
6	0.64	2.863	45.4
7	0.76	1.902	40.8
8	0.87	1.523	38.4
9	0.83	2.750	45.0
10	0.99	4.268	48.6
11	0.73	3.243	46.6
12	0.85	3.437	47.1
13	0.85	2.742	45.0
14	0.91	1.606	38.9
15	0.87	2.644	44.6
16	0.90	4.639	49.0
17	0.73	2.573	44.3
18	0.78	3.351	46.9
19	0.99	3.490	47.3
20	0.98	3.340	46.9
21	0.94	1.593	38.9
22	0.99	1.963	41.2
23	0.96	2.278	42.9
24	0.98	3.342	46.9
25	0.97	2.182	42.4

Table 2: A total cut score estimate based on each item



Feedback to the judges on the accuracy of their probability ratings

In the standard Angoff procedure, the item cut scores are summed to give a total cut score. This total cut score can be converted into a person ability measure via a conversion table, as shown in Figure 1. In addition, an item difficulty estimate in logits is available for each item from the IRT analysis.

Then Equation 1 can be used to estimate the probability of success on each item and compare it with the judges' estimated probability of success (the Angoff rating). This is shown in Table 3 below for the first 30 items.

Such a table can be presented in item order (as shown) above or sorted in order of the discrepancy between the IRT probability and the judges' probability. The latter would clearly show the judges the items where their judgements were most discrepant from the results of the IRT model. Most Angoff procedures in recent times are multi-stage. This statistical feedback would give the judges a chance to rethink some of their ratings in the second stage. For example, Item 16 (shaded in the table) is a very difficult item according to the IRT analysis, with a difficulty rating of 2.44 logits. The predicted IRT probability of success was only 0.55 for the Band 6 marginal students on this item. However, the judges expected the high-level Band 6 students to perform well on the item, with an average probability of success rating of 0.90. This discrepancy is an indicator to the judges to closely re-examine this item and attempt to determine why it proved to be so difficult in general, and to the high ability Band 6 group, and to adjust their ratings accordingly.

BOOKMARKING PROCEDURES

A newer method of standard setting which does not involve item by item judgements is the Bookmark method (Mitzel et al, 2001). In this procedure the test is analysed by IRT to produce item difficulty estimates and person ability estimates. A criterion probability is then set such that, for students conceived to be at the marginal cut score level, two-thirds of the group would be expected to succeed on the item. The task of the judges is to search through the test for this item—the one with a probability of success of 0.667 for students at the cut score. This probability is termed the response probability (RP) and is commonly set at two-thirds (Reckase, 2000; Mitzel et al., 2001; Buckendahl, Smith, Impara and Plake, 2002).

A second important concept is the *bookmark*. *difficulty location* (*BDL*). Given the difficulty of an item in logits and the response probability, one can determine the *ability level* required for a probability of success on an item *equal to the response probability*. This ability level is the *BDL*. Note that although this measure is called a difficulty location, it is defined as an ability level (the ability and difficulty being measured on the same scale).

The *BDL* is calculated for each item, and is used to rank the items in order in a booklet starting from the lowest *BDL* (corresponding to easy items) to the highest *BDL* (corresponding to difficult items).

To calculate the BDL for the Rasch model, Equation 2 is used. Substituting the response probability (RP) gives the BDL for a particular item:

$$BDL_{j} = \beta_{j} - \ln\left(\frac{1 - RP}{RP}\right). \tag{3}$$

That is $BDL_i = \beta_i + constant$.

For example, for a response probability of twothirds, putting RP = 2/3 in Equation 3 gives

$$BDL_i = \beta_i + 0.69315.$$

However, other response probabilities can be used. Wang (2003) advocates a response probability of 0.5 which (substituting RP = 0.5 into Equation 3) gives

$$BDL_i = \beta_i , \qquad (4)$$

with a constant of zero.

		Probability of being correct for ability at the cut score		
Item	IRT item difficulty	Judges' estimate	IRT estimate	Difference
1	-0.288	0.91	0.95	-0.040
2	1.821	0.82	0.69	0.125
3	0.582	0.83	0.89	-0.061
4	-0.136	0.92	0.94	-0.019
5	-1.161	0.98	0.98	0.002
6	2.280	0.64	0.59	0.055
7	0.758	0.76	0.87	-0.108
8	-0.349	0.87	0.95	-0.085
9	1.141	0.83	0.82	0.018
10	-0.327	0.99	0.95	0.039
11	2.231	0.73	0.60	0.135
12	1.702	0.85	0.72	0.134
13	1.007	0.85	0.84	0.015
14	-0.687	0.91	0.96	-0.057
15	0.772	0.87	0.86	0.002
16	2.442	0.90	0.55	0.353
17	1.561	0.73	0.74	-0.011
18	2.066	0.78	0.64	0.146
19	-1.105	0.99	0.98	0.013
20	-0.324	0.98	0.95	0.025
21	-1.188	0.94	0.98	-0.037
22	-2.632	0.99	0.99	-0.005
23	-0.857	0.96	0.97	-0.012
24	-0.468	0.98	0.96	0.022
25	-1.185	0.97	0.98	-0.012
26	1.630	0.85	0.73	0.119
27	-0.338	0.87	0.95	-0.084
28	-0.178	0.88	0.94	-0.060
29	-0.537	0.93	0.96	-0.026
30	-0.861	0.92	0.97	-0.054

Table 3: Comparison of Judges' and IRT probability estimate	ates
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In the one parameter (Rasch) model, as the *BDL* is equal to the item difficulty plus a constant, *it will rank the items in the same order as the item difficulty*. (With a response probability of 0.5, the *BDL* is exactly equal to the item difficulty.) For other IRT models, the *BDL* will not necessarily rank the items in the same order as the item difficulty.

To see why this is the case, consider a 2parameter IRT model where differing levels of item discrimination are modeled. Consider the item characteristic curves of two items with the *same difficulty value* but with different discrimination values. Suppose that a two-thirds probability of success on the item with the higher discrimination (steeper slope) is reached at an ability to the right of where the two curves cross. Then on the item with the relatively shallow slope (lower discrimination), one must move further to the right along the ability scale before a two-thirds probability of success is obtained. Thus, this item would have a higher *BDL* than the more discriminating item, even though the two items had equal difficulty values.

High ability students would tend to find the less discriminating item more difficult than the other item, while low ability students would tend to find the less discriminating item easier than the other item.

Booklet of sorted items

A *BDL* value is calculated for every item and the items are sorted in ascending order by this measure and printed in a booklet. Judges work through the booklet until they come to an item in which they consider the marginal candidates would have a two-thirds probability of success. An example of part of such a booklet is shown below in Figure 3. In addition to the sorted items, other information could also be provided to the judges, depending on the philosophies of the standardsetting organisation.

For example, the judges could be supplied with the proportion correct of the total candidature on the item as an easily understood indicator of the item's easiness. This norm-referenced data is often useful to the judges. However, although there is usually a close inverse relationship between an item's proportion correct and the BDL they will not necessarily arrange the items in the same order. In addition, one could supply the estimated total cut score that would correspond to the marginal candidate Systems which stress the criterionability. referenced nature of the standards-setting may wish to omit the proportion correct and the estimated total cut score so that the judges' decisions are based solely on their mental image of the marginal candidates and their experience of how such students would typically perform on such an item.

In Figure 3, a judge has placed the bookmark between Item 9 and Item 17. This reflects the judgement that on Item 9, the target marginal students would be expected to succeed with greater than two-thirds probability. However on Item 17, the marginal students would be expected to succeed with two-thirds or less probability.

Table 4 shows a subset of the items in ascending order of *BDL*, based on the response probability of two-thirds. As noted before, there are some minor inconsistencies between the proportion correct and the *BDL* (the latter giving the same order as the IRT difficulty)—for example, Item 2 is slightly more difficult than Item 49 according to the IRT difficulties, but 23% of the candidature were correct on Item 2 compared to 22% on Item 49. The corresponding total cut score is obtained from the *BDL* by using the conversion table shown in Figure 1.

In practice, each judge would place a bookmark *independently* in the first stage of the standard setting. Then usually there would be consultation between judges and an opportunity to change the bookmark position for each judge. To obtain a single bookmark position and total cut score, the *BDLs* just above each judge's bookmark are averaged across judges, and this average (in logits) is then converted to a total cut score by the Figure 1 conversion table.

Item Mapping

A variant of the bookmarking procedure is called item mapping, in which a histogram visual display is used to present the data in a more compact format. As presented by Wang (2003), this technique uses the one parameter (Rasch) model, using the *item difficulties* to order the items, with a response probability of 0.5. This use of the Rasch model with an RP of 0.5 simplifies matters conceptually as it removes any need for the concept of the *BDL*. In this case the *BDLs* are equal to the item difficulties (see Equation 4), so the whole process can be explained to the judges in terms of the item difficulties.

This procedure uses the item difficulty data from Table 4, but instead of presenting it as a table, it is presented as a histogram. A linear transformation is applied to the item difficulties to transform them into an arbitrary scale, but one that seems more meaningful to the judges than the logit scale. At the same time this transformation is used to coarsen the

scale by clumping some adjacent item difficulties into the one value, so that the histogram fits onto a single page. For example, the item difficulties presented in Table 4 were first multiplied by 4, and then 40 was added to this product. The resulting transformed difficulties were then rounded to the nearest integer. They are then plotted as a histogram as shown in Figure 4, with the height of the columns being the number of test items on the rounded difficulty value, and with the item ID numbers being shown in each column.

The judges are able to scan the columns of the histogram, noting the items in each column, and determine the column where the marginal band candidates are considered to have a 50:50 chance of being correct on such items (RP=0.5). Once a judge has tentatively placed a bookmark, this sets an ability level. Given this ability level, the probability of success of the marginal band candidates on nearby items can be found from Equation 1 and given to the judge as additional information to help confirm the judgement.

This procedure requires that the judges be familiar with the items, so that a booklet that sorted the items in IRT difficulty order, as in Figure 3, would still seem a desirable requirement. With items of similar difficulty printed next to each other in the booklet, the judges would not have to turn pages of the test to locate items that appear together in the one histogram column.

Can the item mapping procedure be used with response probabilities other than 0.5? It can, but the explanation of the process to the judges is more complicated with BDLs being used instead of item difficulties. Instead of linearly transforming the item difficulties, it is the BDLs that are transformed. For example in Table 4, a BDL column corresponding to a response probability of twothirds is given, immediately to the right of the item difficulties column. These BDL values can be linearly transformed and presented as a histogram similar to that in Figure 4. The judges then attempt to find the column where the probability of success on the items in the column is two-thirds for the marginal band candidates.

CONCLUSIONS

This paper has indicated four ways in which IRT could be used to improve standard setting. The first three methods are consistent with an Angoff multi-staged approach while the last method and a variant use the bookmarking technique. In each case, some useful norm-referenced data has been added to the IRT data. Whether or not this additional data is acceptable in some educational systems may depend on the extent to which emphasised independently of standards are performance. Such educational systems may wish to suppress this norm-referenced data, or to introduce it at a different stage. For these methods to be of use, it is important that a representative sample of student data is available at the time when judging is taking place. In systems where time pressure in reporting results is an issue, these procedures may not be practicable.

The first method is used to provide data before the judges make (or endorse) Angoff item probability estimates. Before a single judgement has been made, the judges are supplied with a table showing all the total scores and, for each score, the probability of success on every item for the candidates gaining that score. In this technique, the judges are forming a mental image of the marginal candidates and are focusing on rows of data, which seem to reflect the item probability estimates that such a group would be expected to obtain. This has several appealing features. It is probably quicker than the normal item by item Angoff ratings. It demonstrates the differences in item difficulty (as shown by the differences in probability of success) at different points of the scale. It provides IRT probabilities of success based on a clearly stated model, rather than judges estimates, which can be For evidence of the possible quite fallible. inaccuracy of such estimates see Bejar, 1983; Mills and Mellican, 1988; Shepard, 1995; Goodwin, 1999. At the same time, if the educational system is such that it prefers to leave the final decision on the probability estimates to the judges, the data provided may be used to inform the judges' decisions rather that dictate it. The judges would then use the data as a guide in submitting their own probability estimates.



Figure 3 :Example layout of items arranged in order of ability at which P=0.667 and the selection of a bookmark

Item	Proportion	IRT item	BDL value	Corresponding
	correct	difficulty	(RP = 0.667)	Total Cut Score
30	0.70	-0.861	-0.168	23.8
23	0.70	-0.857	-0.164	23.8
38	0.68	-0.767	-0.074	24.7
14	0.67	-0.687	0.006	25.5
29	0.65	-0.537	0.156	26.9
45	0.63	-0.494	0.199	27.3
24	0.63	-0.468	0.225	27.5
8	0.61	-0.349	0.344	28.7
27	0.60	-0.338	0.355	28.8
10	0.60	-0.327	0.366	28.9
20	0.60	-0.324	0.369	28.9
1	0.59	-0.288	0.405	29.2
43	0.58	-0.244	0.449	29.6
28	0.57	-0.178	0.515	30.2
4	0.57	-0.136	0.557	30.6
35	0.56	-0.114	0.579	30.8
48	0.55	-0.064	0.629	31.2
37	0.54	0.008	0.701	31.9
40	0.53	0.043	0.736	32.2
46	0.47	0.323	1.016	34.5
44	0.46	0.384	1.077	35.0
3	0.43	0.582	1.275	36.6
7	0.40	0.758	1.451	37.9
15	0.39	0.772	1.465	38.0
39	0.36	0.897	1.590	38.8
13	0.34	1.007	1.700	39.6
33	0.34	1.029	1.722	39.7
9	0.32	1.141	1.834	40.4
17	0.26	1.561	2.254	42.8
26	0.25	1.630	2.323	43.1
12	0.25	1.702	2.395	43.5
49	0.22	1.803	2.496	43.9
2	0.23	1.821	2.514	44.0
18	0.19	2.066	2.759	45.0
11	0.19	2.231	2.924	45.6
6	0.16	2.280	2.973	45.8
16	0.17	2.442	3.135	46.3

Table 4: A subset of the items arranged in BDL order (RP=0.667) and showing estimated Total Cut Scores



Figure 4: Example of an Item Map

The second method shows the impact of each item probability estimate by converting it to an equivalent total cut score. This gives a vivid way of showing which estimates deviate markedly from the It also suggests the possibility of majority. determining a final total cut score by referring to this distribution of total cut scores and choosing an appropriate statistic. For example, the judges may wish to choose the cut score at the 25th percentile, rather than the median, on the grounds that the latter is too severe a level for identifying the marginal candidates-using the median would be discarding half their cut score estimates for competency as being too low. This type of decision is arbitrary but defensible, just as other elements of standard setting are arbitrary (for example, the setting of the response probability).

The third method is well suited to traditional multi-staged Angoff procedures. The item probabilities are estimated by the judges and then summed to get a total cut score. IRT then converts that total cut score into an ability estimate and then determines the probability of success on each item for persons of that ability. These probabilities are then compared to those of the judges to see if there are any major discrepancies. The judges are then free to modify their probability estimates at the next stage.

The Bookmark procedure relies on IRT to order the items. They are ordered in terms of the ability required to have a probability of success on an item equal to the response probability (set commonly at two-thirds) – that is, the *BDL* order. So the easy items appear first in a booklet, getting progressively more difficult as one goes through the booklet. For example, on the very easy items, the judges may estimate the probability of success for the marginal candidates at 0.90 or higher. But as the items get harder, this probability would steadily decrease until a stage is reached where the judges think the candidates they have in mind would have only a two-thirds probability of success. At this point they place a bookmark. The ability at this point can then be converted into a total cut score on the raw mark scale if desired, as this scale is most easily interpretable by the judges. The ordered question booklet may also be presented with normreferenced data next to the items, for example, the proportion correct in the population and/or the equivalent total cut score if the bookmark were to be placed at that point. Some systems may consider that the latter could bias the decisions of the judges.

This paper has used the one-parameter logistic (Rasch) model to illustrate the way standard setting could be assisted by IRT. However, other systems may prefer to use more complex IRT models such as the three-parameter logistic model. Such applications differ from Rasch models in that there is not a unique one-to-one relationship between total score and ability. Under Rasch modeling, there is a *line of relationship* between ability and total score—for a given ability there is one associated total score (as in Figure 1). In non Rasch models, for a given ability there is a distribution of total scores, and vice versa. For these models the curve in Figure 1 would tend to follow the same shape but

would resemble a scatterplot, with multiple abilities for each total score.

In such cases, the total score scale can be often replaced by the ability scale for the methods presented in this paper. For example, the probability data in Table 1 could be generated using a non Rasch model, but the far left column would be replaced by an ability scale. The judges could still encircle the appropriate probability estimates and find the row that best expressed the desired standard of achievement. This would then define a standard in terms of the ability scale. If desired, this scale could be linearly transformed to a scale more closely resembling the raw mark scale. Similarly for the Table 2 method, the corresponding total cut score could be removed and replaced by a linearly transformed ability scale.

The procedure based on the Table 3 data, however, is incompatible with non Rasch models. After summing the Angoff ratings, a total cut score on the raw mark scale is obtained. There is no oneto-one relationship between this cut score and ability-this cut score could be associated with many ability scores, depending on the particular items on which a student was correct. Having said this, a conversion between the raw mark scale and the ability scale can always be obtained through approximate methods (e.g. equating percentiles in the ability and raw score distributions). As the judges generally understand and prefer a raw mark scale, some systems may wish to convert to the raw mark scale, even though it is against the spirit of non Rasch models.

A second issue concerns Angoff standard setting with constructed response items. There are Rasch models that accommodate constructed response items (for example, Andrich's extended logistic model in the RUMM software package; Master's (1982) partial credit model). These models give a one-to-one relationship between total score and ability, as shown in Figure 1. On a constructed response item the Angoff judges estimate a cut score *as a mark*, rather than as a probability. Despite this difference, useful IRT data can be provided to the judges from such packages. For example, a table similar to Table 1 can be constructed with the total mark and percentile columns, but with the probabilities for each item replaced by *expected scores* (which are obtained from the software). Suppose for example that Item 1 had a maximum possible score of 10. Then the table might show that students gaining a total score on the test of 85 (/100) had an expected score of 7.8 (/10) on Item 1. The judges could encircle the expected score for Item 1 that is closest to their cut score, and then repeat the process for Item 2 etc until they were confident of selecting the appropriate row that best reflected the pattern of encircled cut scores. This row then gives the total cut score.

The bookmarking method may also be performed with constructed response items, with Rasch or non Rasch models. Whereas multiple choice or dichotomously scored items appear only once in the ordered test booklet, constructed response items appear several times depending on the number of score points available. Associated with each score point is a BDL-such an item with score points of 0, 1, 2, 3 would appear three times in the booklet, once for each non zero score point. The BDL for 1 would appear first in the booklet, the BDL for 2 would appear at a more difficult location, and the BDL for 3 would appear at the most difficult location of the three points. Suppose the response probability is two-thirds. Then the BDL for a score point in a polychotomous item is the ability level required to have a two-thirds probability of gaining that score or above.

The Bookmark procedure has an advantage over the Angoff method in that it avoids the item by item judgements that can be tedious and difficult for the judges. However there are some technical issues to consider in this procedure, relating to the choice of the response probability and the choice of IRT model. As the Bookmark procedure involves an ordering of the items, Beretvas (2004) has shown how the choice of IRT model and response probability may affect the rank order in which the items would be presented (the BDL). In Beretvas' data set, Spearman correlations between bookmark difficulty locations were computed for various combinations of IRT model and response probability. These were generally above 0.90 but did not give perfect agreement. Given that there is often considerable variation in where judges set

their bookmarks, with the final cut score being the average of the logit values, it is likely that the effect of slightly differing rank orders of the items would not have a great effect on the cut score. However, this would be a useful area for future research.

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