# Using Principles of Measurement to support score interpretation

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# 2013-2014 Technical Manual for Minnesota's Title I and Title III Assessments

**Understanding Measurement Error** 

When interpreting test scores, it is important to remember that test scores contain some amount of measurement error. That is to say, test scores are not infallible measures of student characteristics.

Because measurement error tends to behave in a fairly random fashion, when aggregating over students, these errors in the measurement of students tend to cancel out. Chapter 8, "Reliability," describes measures that provide evidence indicating measurement error on Minnesota assessments is within a tolerable range. Nevertheless, measurement error must always be considered when making score interpretations.

#### Using Objective/Strand-Level Information

Strand or substrand level information can be useful as a preliminary survey to help identify skill areas in which further diagnosis is warranted. The standard error of measurement associated with these generally brief scales makes drawing inferences from them at the individual level very suspect; more confidence in inferences is gained when analyzing group averages. When considering data at the strand or substrand level, the error of measurement increases because the number of possible items is small. In order to provide comprehensive diagnostic data for each strand or substrand, the tests would have to be prohibitively lengthened. Once an area of possible weakness has been identified, supplementary data should be gathered to understand strengths and deficits.

$$SEM = 12.1\sqrt{(1 - 0.88)} = 4.19$$
 (8.5)

Placing a one-SEM band around this scale score would result in a score range of 346 to 554 (that is, 350  $\pm$  4.0). Furthermore, in the case of unbiased scores and if measurement error is normally distributed, then the *true scores* for approximately 68% of test takers would fall in the interval band created by adding and subtracting one SEM from their reported score. Thus, the chances are better than 2 out of 3 those students with an observed score of 350 and SEM = 4 would have an estimated true score within the interval 346–354. This interval is called a confidence interval or confidence band. By increasing the

#### Measurement Error for Groups of Students

As is the case with individual student scores, district, school and classroom averages of scores are also influenced by measurement error. Averages, however, tend to be less affected by error than individual scores. Much of the error due to systematic factors (i.e., bias) can be avoided with a well-designed assessment instrument that is administered under appropriate and standardized conditions. The remaining random error present in any assessment cannot be fully eliminated, but for groups of students random error is apt to cancel out (i.e., average to zero). Some students score a little higher than their true score, while others score a little lower. The larger the number in the group, the more the canceling of errors tends to occur. The degree of confidence in the average score of a group is generally greater than for an individual score.

# 2013-2014 Yearbook Tables for Minnesota's Title I and Title III Assessments

#### 2014 MCA-III Score Distribution

#### Grade 03 Reading

Scale	Online	Paper S.F.M	Frequency	Percent	Cum.	Cum.	Percentile	Achievement
335	5.2	5.1	726	1.2	12464	20.0	19	D
336	5.1	5.1	775	1.2	13230	20.0	21	D
337	5.1	5.0	809	1.2	14048	21.5	22	D
220	5.0	5.0	770	1.5	14040	22.0	22	D
220	5.0	5.0	010	1.2	14010	25.0	23	D
240	5.0	5.0	019	1.5	15057	25.1	24	D 0
340	5.0	5.0	040	1.4	10465	20.5	20	P
341	5.0	5.0	921	1.5	1/406	27.9	27	P
342	5.0	5.0	967	1.6	18373	29.5	29	P
343	5.0	5.0	1001	1.6	19374	31.1	30	Р
344	5.0	5.0	1023	1.6	20397	32.8	32	P
345	5.0	5.0	1066	1.7	21463	34.5	34	Р
346	5.0	5.0	1118	1.8	22581	36.3	35	Р
347	5.0	5.0	1152	1.8	23733	38.1	37	Р
348	5.0	5.0	1170	1.9	24903	40.0	39	Р
349	5.0	5.0	1189	1.9	26092	41.9	41	Р
350	5.0	5.0	1313	2.1	27405	44.0	43	м
351	5.0	5.0	1212	1.9	28617	46.0	45	м
352	5.0	5.0	1251	2.0	29868	48.0	47	м
353	5.0	5.0	1255	2.0	31123	50.0	49	м
354	5.0	5.0	1290	2.1	32413	52.0	51	м
355	5.0	5.0	1284	2.1	33697	54.1	53	м
356	5.0	5.0	1329	2.1	35026	56.2	55	м
357	5.0	5.0	1247	2.0	36273	58.2	57	М
358	5.0	5.0	1281	2.1	37554	60.3	59	м
359	5.0	5.1	1357	2.2	38911	62.5	61	м

#### 2014 MCA-III Score Distribution

#### Grade 08 Mathematics

Scale Score	Online S.E.M.	Paper S.E.M.	Frequency	Percent	Cum. Frequency	Cum. Percent	Percentile Rank	Achievement Level
847	3.1	3.1	1577	2.7	20574	34.9	34	P
848	3.1	3.0	1525	2.6	22099	37.4	36	P
849	3.1	3.0	1668	2.8	23767	40.3	39	P
850	3.1	3.0	1666	2.8	25433	43.1	42	М
851	3.0	3.0	1684	2.9	27117	45.9	45	М
852	3.0	3.0	1795	3.0	28912	49.0	47	М
853	3.0	3.1	1742	3.0	30654	51.9	50	М
854	3.0	3.1	1779	3.0	32433	55.0	53	М
855	3.0	3.1	1760	3.0	34193	57.9	56	М
856	3.0	3.2	1717	2.9	35910	60.8	59	М
857	3.0	3.2	1777	3.0	37687	63.9	62	М
858	3.0	3.2	1744	3.0	39431	66.8	65	М
859	2.9	3.3	1656	2.8	41087	69.6	68	М
860	2.9	3.3	1614	2.7	42701	72.4	71	М
861	2.9	3.4	1598	2.7	44299	75.1	74	E
862	3.0	3.4	1492	2.5	45791	77.6	76	E

#### 2014 MCA-III Subscale Correlations

#### Grade 08 Mathematics

Pearson Correlation Coefficients									
Total Scale Score	Number & Operation	Algebra	Geometry & Measurement	Data Analysis & Probability					
1.00	0.84	0.95	0.79	0.75					
0.84	1.00	0.75	0.62	0.57					
0.95	0.75	1.00	0.71	0.66					
0.79	0.62	0.71	1.00	0.54					
0.75	0.57	0.66	0.54	1.00					
	Pears Total Scale Score 1.00 0.84 0.95 0.79 0.75	Pearson Correlation C   Total Scale Number   Score & Operation   1.00 0.84   0.84 1.00   0.95 0.75   0.79 0.62   0.75 0.57	Pearson Correlation Coefficients   Total Scale Number Algebra   Score & Operation Algebra   1.00 0.84 0.95   0.84 1.00 0.75   0.95 0.75 1.00   0.79 0.62 0.71   0.75 0.57 0.66	Pearson Correlation Coefficients   Total Scale Score Number & Operation Geometry Algebra Geometry & Measurement   1.00 0.84 0.95 0.79   0.84 1.00 0.75 0.62   0.95 0.75 1.00 0.71   0.79 0.62 0.71 1.00   0.75 0.57 0.66 0.54					

#### MCA-III Summary Statistics

#### Grade 08 Mathematics - Online

Total							
Scale	Range of Items	N	Mean	SD	Marginal Reliability		
Total Scale Score	42	51469	851.80	13.70	0.93		
Number & Operation Strand	6-8	51469	5.06	1.78	0.69		
Algebra Strand	18-29	51469	5.19	1.96	0.84		
Geometry & Measurement Strand	6-8	51469	5.17	1.68	0.61		
Data Analysis & Probability Strand	6-7	51469	5.06	1.69	0.51		

### 2014 MCA-III Subscale Correlations

### Grade 03 Reading

Pearson Correlation Coefficients							
	Total Scale						
	Score	Literature	Information				
Total Scale Score	1.00	0.94	0.93				
Literature	0.94	1.00	0.80				
Information	0.93	0.80	1.00				

#### 2014 MCA-III Summary Statistics Reports

#### Grade 03 Reading - Online

Total								
Scale	Range of Items	Z	Mean	SD	Marginal Reliability			
Total Scale Score	48	24211	352.23	20.50	0.88			
Literature	21-27	24211	5.04	1.90	0.81			
Information	21-27	24211	5.06	1.94	0.80			

 $r_{xy} \leq \sqrt{r_{xx}r_{yy}}$ 



CONVERSION RELEASE

### **CORE IDEA**

 Assessments are not the end of the teaching and learning process; they're the starting point.

... we should not teach and then write an assessment to match; instead, we should create a rigorous and demanding test and then teach to meet its standards

### **CORE IDEAS: Interim Assessments**

• Start from the end-goal exam.

...

Align the interim assessments to the end-goal test.

### **Analyze the Interim Assessment or End-Goal Test**

Acquire the closest version that you can find of your state test, interim assessment, or other yearend assessment by which your students' learning will be measured.

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